Conflict Resolution in Advice Taking and Instruction for Learning Agents

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Abstract

An extended version of this paper is available as an IBM Research Report *via the above address, including as a postscript file on the World Wide Web. It includes a review of relevant concepts of defaults and precedence from non-monotonic logical formalisms, as well as a variety of other material, especially discussion.*

We raise and discuss several issues of advice taking and instruction, including: the challenges of very small samples of opinion, and of assimilation with a large, complex prior knowledge base. We focus especially on the problem of conflicting yes/no rules. We observe the availability of natural kinds of information, e.g., authority, reliability, freshness, and specificity, as the basis for reasoning about precedence. By precedence we mean in the sense of resolving conflicts between rules on the basis of qualitative ordinal information.

We propose an approach to this problem of conflict: via defaults and reasoning about such precedence, drawn from knowledge representation and commonsense reasoning. We initially developed this approach in previous work. Here, we elaborate it, abstract it to a more conceptual level, and present it for a machine learning audience. Also, we abstract it away from the details of, and dependency on, one particular non-monotonic logical formalism.

We see the value of this approach not as being all-embracing, but as providing a step towards elements of future approaches to advice-taking and instruction.

1 Challenges

1.1 Assimilation with Prior Knowledge

From the machine learning viewpoint, a distinguishing characteristic of learning by advice-taking or instruction is its close relationship to learning in the presence of a **large, complex prior knowledge** base. This is particularly important now that practical intelligent agents are being realized that are equipped with substantial knowledge bases.

The relationship to learning with prior knowledge is bidirectional. On the one hand, advice-taking and instruction provide a conduit for agents to acquire substantial, and perhaps expressively complex, knowledge bases. On the other hand, substantial knowledge bases are typically necessary for agents to usefully exploit the advice and instruction they receive.

A major challenge for an agent taking advice or instruction is to **assimilate** the advice or instruction into its own beliefs and mental state, in a rationalized and coherent manner.

1.2 Importance of Yes/No Rules and Facts as Knowledge Representation

An important form of knowledge representation is **rules plus facts** of the kind expressible in monotonic first-order logic, perhaps augmented by basic non-monotonic mechanisms, negation-as-failure cf. logic programming (e.g., Prolog) and simple inheritance with exceptions (e.g., frame-based systems). Such **yes/no** (as opposed to probabilistic or fuzzy) rules and facts have been widely used in knowledge-based systems generally, not just in intelligent agents. They have been found useful as well in logic programming languages. Their advantages compared with probabilistic or fuzzy representations include relative conceptual simplicity, as well as relative computational simplicity.

1.3 Learning from Very Small Samples of Opinion

One of the hard-won lessons of applied AI is that knowledge acquisition is often difficult. An implication is that agents should often be designed to make the most of what advice they can obtain.

Humans often use knowledge on matters about which they have received only a very small number of opinions (pieces of advice): e.g., 1 or 2 or 3. This is important especially in realms where direct experience (exemplars) is not available, or is costly. Humans often act when they have received only one piece of advice, e.g., in an office organization or other social situation with a fair degree of trust. In such situations of very small "samples", most inductive learning methods, which are typically statistical in flavor, do not have much help (or confidence) to offer. The work of [Maes, 1994] [Lashkari *et al.*, 1994] is an interesting approach, viewable as advice-taking, which exploits a community of agents via communicating example sets. Nearest-neighbor inductive learning then becomes the basis for the advice-taker's beliefs. However, a drawback is that this kind of advice-taking requires, in effect, large samples, and/or for a great deal of knowledge to be encoded in the distance function (i.e., similarity measure).

An implication of the foregoing is that we should enable agents to cope with situations of reasoning and acting where they cannot presume that they will get lots of experiential feedback to furnish a basis for inductive-style learning. Rather, in many situations, an agent should mainly trust what information it manages to learn from communication.

2 Problems: Conflict

2.1 Advice Taking

With rules form of knowledge (in the sense discussed earlier), an important aspect of assimilation is handling **conflict** between the rules (and facts) that are received as various pieces of advice or instruction. Sources of information might include messages from other agents (e.g., humans), reading texts, etc..

We expect that a basic feature of agent life, as of human life, is that one cannot believe everything that one is told. Not only may advice be incorrect; e.g., it may contradicted by direct experience. Worse, different sources of advice information may contradict each other, or even themselves. How is an advice-taking agent to maintain a consistent, yet usefully actionable, set of beliefs, then?

In human life, such conflict (disagreement) occurs often. For example, I once got conflicting advice from two bureaucrats in my company about how to get the light bulb repaired in my office. As another example, the U.S. Presidents have often gotten conflicting advice from their immediate staffs about which issues deserved attention, or which political maneuvers would be most expedient.

2.2 Instruction and Authoring

Instruction can be viewed as how to assimilate one or more pieces of advice from a single source agent into the beliefs of a learning recipient agent. Often these different pieces of advice are received at different times. An interesting pragmatic first step towards this problem is when the single source agent is a *human*, e.g., a user communicating through a user interface. Like an automatic agent, a human source may have only a rough knowledge of what language, ontology, commonsense/background/context knowledge, and interface format are appropriate to communicate to the recipient agent. E.g., the human may be a "lay" (non-programmer) user trying to instruct the recipient agent to act on her behalf.

When the source agent is a human, instruction can thus be viewed as *authoring*, i.e., the incremental specification of a belief set (i.e., creation of a knowledge base) that the recipient agent should hold.

A key, well-known problem in knowledge-based system development, generally, is the "knowledge acquisition bottleneck". In rule-based systems, for example, even for expert programmers it is difficult to specify, test, and debug a set of rules; and much more difficult for lay users to do such authoring. A major reason for such difficulty is the potential for *conflicting* interaction between rules within a group of rules. A common situation is that a special-case rule may contradict a more-general-case rule.

For example, consider an application of e-mail filtering for importance. I might tell my Mailbot "if the message is from a store, then it's low importance" (rationale: it's probably useless junk mail). And I might tell it further that "if the message is from a store from which I'm awaiting an order, then it's high importance" (rationale: it's probably about my order and my order is probably important). These two rules conflict in the case of a message from a store from which I'm awaiting an order. The second rule is more specific. Commonsense style of instruction suggests that the second rule should win the conflict. This basis for precedence (winning) between rules is known as **specificity**: the antecedent of the second rule is a condition strictly subsumed by (i.e., more specific than) the antecedent of the first rule. This kind of implicit presumption of specficity precedence has been studied extensively in the non-monotonic reasoning community, e.g., [Touretzky, 1986].

In developing rule bases, this potential for conflict partly arises after knowledge is encoded, due to in-

ference and representation mechanisms that involve logical non-monotonicity, e.g., the use of negation-as-failure and inheritance with exceptions. However, even beyond such programming mechanisms, this potential for conflict also arises during the process of encoding knowledge, due to unforeseen contradictions between "draft" rules. In my view, this is because humans often think in a manner that, in effect, involves logical non-monotonicity: e.g., often special-case rules are *implicitly* regarded as overriding more-general-case rules. Either way (during or after encoding knowledge), such logical non-monotonicity causes non-modularity and complexity of the behavior of incremental changes to the set of rules.

This non-modularity and difficulty of incremental development can be viewed as a difficulty in assimilating instruction, i.e., in assimilating pieces of advice from a single source. (Actually, as a practical matter, knowledge-based systems are often developed from the interleaved contributions of *several* human sources of knowledge, i.e., of programming or domain expertise. These sources sometimes conflict with each other.)

3 Approach: Advice as Defaults with Prioritization-type Precedence

3.1 Our Focus: Rule Beliefs and Conflict Handling

Next, we discuss our approach to handling and resolving conflicts in advice taking and instruction.

We address all the challenges and problems discussed earlier: assimilation with substantial prior knowledge, advice in the form of yes/no rules as well as facts, and the presence of conflict.

Methodologically, as a first step, we restrict our focus to learning beliefs rather than plans or goals.

3.2 Inspiration: Human Tactics in Advice Taking

Our approach is based on employing the knowledge representation tools of defaults with prioritization-type precedence. It is inspired by our observation of two tactics people employ.

First, humans often employ the tactic of treating advice sources as credible, but allowing advice information to be defeasible (retractable). That is, they treat advice as working belief, which can be overridden by other advice and direct experience. This suggests the first element of our approach: to **represent advice as default-status premise belief**.

Second, when faced by contradictory conflicts between two (or more) pieces of advice, humans often employ the further tactic of resolving the conflict definitively in favor of the advice that arises from the *source* that has greater precedence. The structure of such precedence often has a qualitative, ordinal flavor, similar to that of the concepts of prioritization-type precedence developed in non-monotonic logical formalisms.

Indeed, some beliefs are about **which sources to believe more** on what subjects in which circumstances. These beliefs themselves may arise from taking advice from multiple, sometimes-conflicting sources. Such beliefs about precedence are thus not only important but also **defeasible**.

All this suggests the second element of our approach: to **represent and reason defeasibly about prioritization-type precedence, including about sources**.

3.3 Bases for Precedence Among Advice Defaults

There are several natural kinds of available information that can furnish the basis for such precedence orderings between pieces of advice or instruction. These bases for such precedence include:

- specificity,
- freshness,
- authority,
- reliability,

(or, more generally, some other property). That is, a precedence ordering among advice is derived from a precedence ordering among sources, which in turn is derived from properties of sources such as authority, reliability, and freshness. More generally, the precedence among sources may also be relative to the subject area of the advice, or to the situations, e.g., times, in which advice is offered or to which it applies.

By **specificity**, we mean the sense we discussed earlier (section 2): instruction or advice which covers a more-specific case takes precedence over that which covers a more-general case.

Specificity is especially relevant and available as a basis for precedence between two pieces of advice taken from the same source, e.g., in instruction.

By **freshness**, we mean the recency of the advice and/or the information upon which the advising source bases that advice. E.g., in classical database updating, there is typically a presumption that more recent updates override previous information. E.g., advice received today from one's broker to buy a particular stock is typically given precedence over advice received from her last month to sell that stock.

Like specificity, freshness is especially relevant and available as a basis for precedence between two pieces

of advice taken from the same source, e.g., in instruction. But it applies between sources as well. E.g., advice from a credible stock broker received today is typically given precedence over advice from a credible stock broker received three years ago.

By **authority**, we mean in the legal and organizational senses. For example, federal law takes precedence over state law; directives from the head of an organization take precedence over those from subordinates.

By **reliability**, we mean in the sense of accuracy or likelihood of correctness. For example, I believe the New York Times newspaper to be a more reliable source than the New York Post and the Village Voice newspapers, which in turn I beleve to be more reliable than the National Enquirer newspaper. For example, Mikey the elementary school student believes his parents to be more reliable sources than his schoolfriends and his schoolteachers, and believes those to be more reliable in turn than his schoolenemies.

Reliability may be, in turn, based on (inferred from information about) **expertise**, **judgment**, etc..

Authority and reliability are especially relevant and available as bases for precedence between different sources.

3.4 Essence of Approach

In the advice-taker:

1. Represent advice to be the content of utterance information from a credible source. A source which is adequately honest and competent is usefully trustworthy.
2. Represent each piece of advice as a default premise belief. Each default premise belief has an associated label.
3. Resolve conflicts between advice using precedence between the defaults.
4. Represent precedence explicitly, so that it can be reasoned about automatically by the advice-taking agent.
5. Represent sources explicitly, including their relationship to the advice they give, e.g., to the labels of the associated defaults.
6. Represent the bases for precedence explicitly, e.g., information about the authority, reliability, freshness, and specificity of sources (and thus their advice) relative to subjects and situations / times.

   Likewise, one can extend this to represent the bases for credibility explicitly, e.g., information about the honesty and competence of sources (and thus their advice). However, credibility is less of an immediate issue for handling conflict than precedence is.

Our approach has several attractive features. By treating each piece of advice as a premise default, any piece involved in conflict can be overridden as a conclusion. Overall consistency is preserved when conflict arises, whether or not it is definitively resolved. Information of kinds that are available and natural for knowledge acquisition is exploited as the basis for resolving conflicts.

3.5 Formulation in DAP Circumscription

In previous work, we began investigation and development of our approach to advice-taking. [Grosof, 1993b] [Grosof, 1993a] There, we employed a variant of circumscription as the non-monotonic logical formalism. We invented this formalism, Defeasible Axiomatized Policy (DAP) circumscription, mainly for this specific purpose. We developed the theoretical aspects of the formalism, including a sketch of inferencing algorithms [Grosof, 1993a].

This work builds upon our other previous work relating learning and non-monotonic reasoning [Grosof, 1992b] [Grosof, 1992a] [Grosof, 1993c], which is largely based on our DAP circumscription formalism, and on our new inference algorithms for prioritized default reasoning expressed in circumscription [Grosof, 1992b] [Grosof, 1995a] [Grosof, 1995b].

4 Meta-Language Formulation of our Approach

To illustrate the approach, in the next section we will illustrate it with a detailed example. Preliminary to that, in this section we give a specification notation $\mathcal{PD}$, acronymic for "Precedence plus Defaults". $\mathcal{PD}$ is a meta-language, new with this paper. We will use it to describe the example.

The $\mathcal{PD}$ notation serves two purposes. First, it is simpler, especially for the reader to follow, than the DAP circumscription formalism. Second, it simplies mapping our approach into other non-monotonic logical formalisms. It thus reduces or removes the dependence of our approach on one particular non-monotonic formalism.

In $\mathcal{PD}$, there are two kinds of premise beliefs (axioms): for-sure and default. By a for-sure premise belief, we mean a non-retractable belief of the kind familiar from first-order logic.

Each premise belief has a label as a prefix, enclosed in $\langle\ \rangle$. E.g.,
$\langle Sure \rangle \quad Small(Isaac) \supset \neg Big(Isaac)$
$\langle advice37 \rangle \quad Smiling(Isaac) \supset \neg Cranky(Isaac)$
The label of the first premise above is $Sure$. A premise is for-sure iff it is labelled by the special label $Sure$, as in the first premise above. A premise is default iff it is

labelled by any label other than *Sure*, e.g., *advice*37 in the second premise above. Each default premise's label is required to be unique. The rest of the axiom after the label is called its *formula part*, a formula in a first-order language $\mathcal{L}$. Each label is a constant individual (object) of $\mathcal{L}$. The label is essentially a name for the premise, used in connection with the formal mechanism of precedence. A for-sure premise's formula part is required to be a closed formula (i.e., sentence). A default premise's formula part may be closed, or it may be open, i.e., include free (i.e., unquantified, unbound) variables, e.g.,

$\langle BirdSchema \rangle \quad Bird(x) \supset Flies(x)$

An open (i.e., schema) default can be viewed as the collection of all its instances. An instance of an open default is a closed default formed by instantiating (i.e., substituting a possible binding for) each of its free variables. A closed default has one instance: itself. We refer to a default instance by writing the pair $\langle label, t \rangle$, where *label* refers to a default, and t refers to an instantiation of that default's free variables. t may be empty. E.g.,

$\langle Bird, Tweety \rangle \quad Bird(Tweety) \supset Flies(Tweety)$
$\langle Bird, Isaac \rangle \quad Bird(Isaac) \supset Flies(Isaac)$
. . . .

$PRECEDES(label1, t, label2, u)$ means that the default instance $\langle label1, t \rangle$ has higher precedence than the default instance $\langle label2, u \rangle$. ($t$ and u may be empty.) $PRECEDES$ is constrained to be a well-founded, strict partial order, defined over the default instances.

See Appendix A1 for details of how $\mathcal{PD}$ maps to DAP circumscription.

4.1 Defeasible Precedence

The example we give in the next section uses only non-defeasible (i.e., monotonic) reasoning about precedence. Above, we gave a version of $\mathcal{PD}$ sufficient for this expressive fragment. More generally, DAP circumscription can represent *defeasible* (i.e., non-monotonic) reasoning about precedence, as well.

DAP circumscription involves a finite tower of 1 or more meta-levels of reasoning about precedence. $\mathcal{PD}$ can be viewed as one such meta-level. By stacking together several meta-levels, each formulated in $\mathcal{PD}$, $\mathcal{PD}$ can be extended to specify DAP beyond just DAP1.

Next, we list some examples where it is useful to represent *defeasible* precedence.

In an organization, change of authorities (e.g., promotion and demotion of managers) leads to change of the precedence accorded to their recommendations or to their instructions, e.g., by subordinates in following potentially-conflicting demands from superiors.

In law, rulings concern precedence of principles or of jurisdictions, and are themselves reversible by subsequent rulings.

See [Grosof, 1993a] for more examples of advice-taking using reasoning about precedence, including defeasible reasoning about precedence.

5 Example: Repairing a Dim Bulb in a Bureaucracy

A different version of this example appeared in [Grosof, 1993b].

5.1 A True Story

Consider the following true story. Bold type in the remainder of this section indicates the most essential parts of the reasoning in the story. By "essential" here, we mean with respect to the problem addressed in this paper.

One Saturday a few years ago, one of the fluorescent overhead lights in my office at IBM suddenly stopped working. I knew that I had to make some kind of official request for the repair, but I did not know exactly who and how to ask. I thus phoned Security and asked them what was the procedure to officially request the lighting repair. The woman answering the phone told me (**Security advice**) that the procedure was simply to type the command "MAINT" to the local mainframe computer system, then obey the instructions it gave me. **I now believed that this was the correct procedure**; in general, in the past, I had found the Security people to be pretty competent, hence credible. I thus acted by following her advice and did the MAINT command: this turned out to be merely to fill out a structured e-mail message to a relevant IBM bureaucrat in charge of maintenance-type repairs. After I sent the message, the system replied automatically that my request was being forwarded first to my departmental Administrative Assistant (AA), who had to approve the request.

Monday afternoon came, and I was just wondering impatiently about my lighting repair, when I received an e-mail message from my (departmental) Administrative Assistant. In it, she said that she had *not* approved my repair request, that it was inappropriate. She said (**AA advice**) that the correct procedure for requesting the lighting repair was to phone Security and to ask them to officially request on my behalf to the building landlord (a separate, non-IBM company, named Robert Martin), to have their maintenance people come and fix it. ("Classic!", I mumbled to myself.) **I now believed that this was the correct procedure. Though it contradicted (i.e., conflicted with) what the weekend Security person had told me, I believed that my AA had more organizational authority than Security on this kind**

of matter and, in the past, had generally also been competent, hence credible (at least as much as Security). **Hence I resolved the conflict definitively (for the time being) in the AA's favor (more precisely, in favor of her advice.) That is, I assigned greater prioritization-type precedence to the AA advice than to the Security advice.**

I thus acted by following the AA's advice. (Though Security again repeated their previous advice, I insisted that they contact the landlord.) Sure enough, within fifteen minutes a landlord maintenance person came to my office and completed the repair.

5.2 Automatable Representation using our Approach

Next, we show in $\mathcal{PD}$ how to represent the beliefs of the advice-taking agent in the above story (a simplified version, of course). This is an automatable representation. (Subsection 6.1 discusses implementation.)

Lower-case arguments indicate variables. *sit* stands for situation. *Sec* stands for Security. My_Pb stands for my particular problem situation. $Light$ stands for lighting repair. $Pesky(subj, sit)$ means that sit is a pesky problem of kind $subj$ that the bureaucracy views as needing to be solved. $Do(proced, sit)$ means that the (unique) correct bureaucratic procedure is $proced$ in situation sit. $MAINT$ stands for the procedure of performing the MAINT command on the mainframe. $Sec_Ask_Landlord$ stands for the procedure of asking Security to ask the landlord. $More_Authority(source1, source2, subject)$ means that $source1$ is more authoritative than $source2$ about $subject$. $Source(a, s)$ means that s is the source of the advice a. $Subject(a, s)$ means that s is the subject of the advice a. $\mid\!\approx\ p$ indicates that the sentence p is non-monotonically concluded from the (current) premise set. $\exists!x. \ldots$ stands for "there exists a *unique* x such that ...".

Before receiving the Security advice or the AA advice, the premise set includes exactly: the uniqueness of names (this can be formulated explicitly as an included for-sure premise), plus

$\langle Sure \rangle \quad \forall subj, sit.\ Pesky(subj, sit) \supset$
$\quad \exists! proced.\ Do(proced, sit)$
$\langle Sure \rangle \quad Pesky(Light, My_Pb)$
$\langle Sure \rangle \quad \forall advice1, advice2, source1,$
$\quad source2, subject, sit.$
$\quad [Source(advice1, source1)$
$\quad \wedge Source(advice2, source2)$
$\quad \wedge Subject(advice1, subj)$
$\quad \wedge Subject(advice2, subj)$
$\quad \wedge More_Authority(source1, source2, subject)]$
$\quad \supset$
$\quad PRECEDES(advice1, sit, advice2, sit)$
$\langle Sure \rangle \quad More_Authority(AA, Sec, Light)$

The Security advice update corresponds to adding the premises:

$\langle Sec_Advice \rangle \quad Pesky(Light, sit)$
$\quad \supset Do(MAINT, sit)$
$\langle Sure \rangle \quad Source(Sec_Advice, Sec)$
$\langle Sure \rangle \quad Subject(Sec_Advice, Light)$

After this update, the advice-taker (non-monotonically) concludes that it should do the MAINT command on the mainframe:

$\mid\!\approx\ Pesky(Light, My_Pb)$
$\quad \supset Do(MAINT, My_Pb)$

which implies

$\mid\!\approx\ Do(MAINT, My_Pb)$

The later, AA advice update corresponds to adding the premises:

$\langle AA_Advice \rangle \quad Pesky(Light, sit)$
$\quad \supset Do(Sec_Ask_Landlord, sit)$
$\langle Sure \rangle \quad Source(AA_Advice, AA)$
$\langle Sure \rangle \quad Subject(AA_Advice, Light)$

After this update, the advice-taker concludes (monotonically) that the AA advice has higher precedence than the Security advice:

$\models\ \forall sit.\ PRECEDES(AA_Advice, sit,$
$\quad Sec_Advice, sit)$

As a result, it retracts the previous non-(monotonic) conclusion above, and (non-monotonically) concludes instead that it should have Security contact the landlord:

$\mid\!\approx\ Pesky(Light, My_Pb)$
$\quad \supset Do(Sec_Ask_Landlord, My_Pb)$

which implies

$\mid\!\approx\ Do(Sec_Ask_Landlord, My_Pb)$

Furthermore, the agent is able to (non-monotonically) **learn an entire rule from conflicting advice** that this is the preferred procedure in further lighting repair situations:

$\mid\!\approx\ \forall sit.\ Pesky(Light, sit)$
$\quad \supset Do(Sec_Ask_Landlord, sit)$

E.g., suppose the premises are further updated with

$\langle Sure \rangle \quad Pesky(Light, Leoras_Pb)$

where $Leoras_Pb$ stands for another (similar) problem of lighting repair that colleague Leora has tomorrow. Then the agent concludes

$\mid\!\approx\ Do(Sec_Ask_Landlord, Leoras_Pb)$

This learned rule is defeasible, e.g., the agent may learn exceptions to it later from further experience or advice taking.

6 Discussion and Related Work

6.1 Implementation Status

The lighting repair example in the last section illustrated our approach and showed how it can be formalized in terms of knowledge representation (beliefs and inferencing both). The results in [Grosof, 1993a], together with those in [Grosof, 1992b] and more recently in [Grosof, 1995a] [Grosof, 1995b], imply how to imple-

ment inferencing for substantial expressive fragments (i.e., sub-classes) of DAP circumscription, and thus of $\mathcal{PD}$. In particular, they suffice to mechanize the lighting repair example.

In current work, we are pursuing the detailed development of more inferencing algorithms for DAP circumscription and thus $\mathcal{PD}$. However, we are also pursuing other non-monotonic formalisms as the avenue to implement the approach, including $\mathcal{PD}$. Our aim is to find a relatively conceptually simple, computationally tractable form of non-monotonic reasoning, together with associated practical (polynomial-time) algorithms. This will then be suitable for "technology transfer", as it were, from the knowledge representation community to the machine learning community, thence to experiment in building advice-taking learning agents using our approach.

6.2 Combining with Direct Experience

A motivation and feature of our approach is that it can assimilate direct experience of the agent, as well as advice or instruction. The agent's direct experience can be represented in $\mathcal{PD}$, for example, by updating with additional premises. E.g., in the lighting repair example, the agent might predict that the correct procedure for Leora's lighting repair problem is to have Security ask the Landlord ($Do(Sec_Ask_Landlord, Leoras_Pb)$), but then learn from direct experience that it is not. Accordingly, the agent might update its premises to assimilate that fact, e.g., :
$\langle Sure \rangle \quad Do(Call_Harry, Leoras_Pb)$.

This capability of our approach is discussed, for example, in [Grosof, 1992a].

6.3 When our Approach is most Suitable

Approaching advice by representing it in a non-monotonic logical system for defaults plus precedence has the usual advantages of being a declarative account and having expressive power.

This is especially helpful when there is significant reasoning with the knowledge, when knowledge and inferencing about the bases for resolving conflicts is itself interestingly contentful.

There are many other relevant issues we did not address here: e.g., operationalization [Gordon and Subramanian, 1993], tight integration with probabilistic-flavor knowledge and techniques, and tight integration with induction, especially from direct experience and large amounts of exemplars.

6.4 Applicability of Approach to Multiple Non-Monotonic Formalisms

We are aware of only two default formalisms that are capable of reasoning about the precedence, e.g., on basis of relative authority. The first one to enable such was DAP circumscription, which we developed for this kind of capability. The second one was developed independently by Brewka [1994], whose formalism, like DAP circumscription, enables reasoning about prioritization. He extends Default Logic, rather than circumscription as we do. Both DAP circumscription and Brewka's formalism need more work to achieve efficient algorithms, guarantees of well-behavior, and better conceptual understanding. As we do with our approach, Brewka remarks that his basic approach should be extensible / applicable to other non-monotonic formalisms that can express defaults and prioritization-type precedence.

A1 Appendix: Mapping of $\mathcal{PD}$ to DAP Circumscription

Our meta-language notation $\mathcal{PD}$ maps straightforwardly to its **interpretation in DAP1 circumscription** (a subset of DAP circumscription), as follows.

Every $\mathcal{PD}$ premise of the form
$\langle Sure \rangle \quad B$
where B is a formula, is mapped into the DAP1 base axiom
B

Every other $\mathcal{PD}$ premise, having the form
$\langle i \rangle \quad D[x]$
(that is, any premise with label other than $Sure$), where D is a formula with (possibly empty) tuple of free variables x, is mapped into the pair of DAP1 base axioms
$\forall x.\ \neg abi(x) \quad \equiv \quad D[x]$
$\forall x.\ N1('abi, x)$
Here, the predicate symbol abi, and its (0-ary function symbol) name object $'abi$, are each introduced as new (unique) symbols into the first-order language.

As a final step, every $PRECEDES(i, t, j, u)$ atom (i.e., primitive sub-formula) is mapped isomorphically to the atom
$R1('abi, t, 'j, u)$
Here, i and j are labels, and t and u are tuples of terms.

The first-order language in the DAP1 interpretation thus differs from that in the $\mathcal{PD}$ premise set, as follows. It does not include the predicate symbol $PRECEDES$. It does include the predicate symbols $R1$ and $N1$, the abi's predicate symbols, and the 0-ary function symbols $'abi$'s.

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